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Research Article

Auditory Sparse Representation for Robust Speaker Recognition Based on Tensor Structure

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This paper investigates the problem of speaker recognition in noisy conditions. A new approach called nonnegative tensor principal component analysis (NTPCA) with sparse constraint is proposed for speech feature extraction. We encode speech as a general higher-order tensor in order to extract discriminative features in spectrotemporal domain. Firstly, speech signals are represented by cochlear feature based on frequency selectivity characteristics at basilar membrane and inner hair cells; then, low-dimension sparse features are extracted by NTPCA for robust speaker modeling. The useful information of each subspace in the higher-order tensor can be preserved. Alternating projection algorithm is used to obtain a stable solution. Experimental results demonstrate that our method can increase the recognition accuracy specifically in noisy environments.

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1. INTRODUCTION

Automatic speaker recognition has been developed into an important technology for various speech-based applications. Traditional recognition system usually comprises two processes: feature extraction and speaker modeling. Conventional speaker modeling methods such as Gaussian mixture models (GMMs) [1] achieve very high performance for speaker identification and verification tasks on high-quality data when training and testing conditions are well controlled. However, in many practical applications, such systems generally cannot achieve satisfactory performance for a large variety of speech signals corrupted by adverse conditions such as environmental noise and channel distortions.

Traditional GMM-based speaker recognition system, as we know, degrades significantly under adverse noisy conditions, which is not applicable to most real-world problems. Therefore, how to capture robust and discriminative feature from acoustic data becomes important. Commonly used speaker features include short-term cepstral coefficients [2, 3] such as linear predictive cepstral coefficients (LPCCs), mel-frequency cepstral coefficients (MFCCs), and perceptual linear predictive (PLP) coefficients. Recently, main efforts are focused on reducing the effect of noises and distortions.

Feature compensation techniques [4–7] such as CMN and RASTA have been developed for robust speech recognition. Spectral subtraction [8, 9] and subspace-based filtering [10, 11] techniques assuming a priori knowledge of the noise spectrum have been widely used because of their simplicity.

Currently, the computational auditory nerve models and sparse coding attract much attention from both neuroscience and speech signal processing communities. Lewicki [12] demonstrated that efficient coding of natural sounds could provide an explanation for both the form of auditory nerve filtering properties and their organization as a population. Smith and Lewicki [13, 14] proposed an algorithm for learning efficient auditory codes using a theoretical model for coding sound in terms of spikes. Sparse coding of sound and speech [15–18] is also proved to be useful for auditory modeling and speech separation, providing a potential way for robust speech feature extraction.

As a powerful data modeling tool for pattern recognition, multilinear algebra of the higher-order tensor has been proposed as a potent mathematical framework to manipulate the multiple factors underlying the observations. In order to preserve the intrinsic structure of data, higher-order tensor analysis method was applied to feature extraction. De Lathauwer et al. [19] proposed the higher-order singular

value decomposition for tensor decomposition, which is a multilinear generalization of the matrix SVD. Vasilescu and Terzopoulos [20] introduced a nonlinear, multifactor model called Multilinear ICA to learn the statistically independent components of multiple factors. Tao et al. [21] applied general tensor discriminant analysis to the gait recognition which reduced the under sample problem.

In this paper, we propose a new feature extraction method for robust speaker recognition based on auditory periphery model and tensor structure. A novel tensor analysis approach called NTPCA is derived by maximizing the covariance of data samples on tensor structure. The benefits of our feature extraction method include the following. (1) Preprocessing step motivated by the auditory perception mechanism of human being provides a higher frequency resolution at low frequencies and helps to obtain robust spectrotemporal feature. (2) A supervised learning procedure via NTPCA finds the projection matrices of multirelated feature subspaces which preserve the individual, spectrotemporal information in the tensor structure. Furthermore, the variance maximum criteria ensures that noise component can be removed as useless information in the minor subspace. (3) Sparse constraint on NTPCA enhances energy concentration of speech signal which will preserve the useful feature during the noise reduction. The sparse tensor feature extracted by NTPCA can be further processed into a representation called auditory-based nonnegative tensor cepstral coefficients (ANTCCs), which can be used as feature for speaker recognition. Furthermore, Gaussian mixture models [1] are employed to estimate the feature distributions and speaker model.

The remainder of this paper is organized as follows. In Section 2, an alternative projection learning algorithm NTPCA is developed for feature extraction. Section 3 describes the auditory model and sparse tensor feature extraction framework. Section 4 presents the experimental results for speaker identification on three speech datasets in the noise-free and noisy environments. Finally, Section 5 gives a summary of this paper.

2. NONNEGATIVE TENSOR PCA

2.1. Principle of multilinear algebra

In this section, we briefly introduce multilinear algebra and details can be found in [19, 21, 22]. Multilinear algebra is the algebra of higher-order tensors. A tensor is a higher-order generalization of a matrix. Let $\mathbf{X} \in \mathbb{R}^{N_1 \times N_2 \times \cdots \times N_M}$ denotes a tensor. The order of \mathbf{X} is M. An element of \mathbf{X} is denoted by $\mathbf{X}_{n_1,n_2,\dots,n_M}$, where $1 \le n_i \le N_i$ and $1 \le i \le M$. The mode-i vectors of \mathbf{X} are N_i -dimensional vectors obtained from \mathbf{X} by varying index n_i and keeping other indices fixed. We introduce the following definitions relevant to this paper.

Definition 1 (mode-d matricizing). Let the ordered sets $\mathfrak{R} = \{r_1, \ldots, r_L\}$ and $\mathfrak{C} = \{c_1, \ldots, c_K\}$ be a partition of the tensors $\mathfrak{N} = \{1, \ldots, M\}$, where M = L + K. The matricizing tensor can then be specified by

$$\mathbf{X}_{(\mathfrak{R}\times\mathfrak{C})} \in \mathbb{R}^{L\times K}$$
 with $L = \prod_{i\in\mathfrak{R}} N_i$, $K = \prod_{i\in\mathfrak{C}} N_i$. (1)

The mode-d matricizing of an Mth-order tensor $\mathbf{X} \in \mathbb{R}^{N_1 \times N_2 \times \cdots \times N_M}$ is a matrix $X_d \in \mathbb{R}^{L \times K}$, where $L = N_d$ and $K = \prod_{i \neq d} N_i$. The mode-d matricizing of \mathbf{X} is denoted as $\mathrm{mat}_d(\mathbf{X})$ or \mathbf{X}_d .

Definition 2 (tensor contraction). The contraction of a tensor is obtained by equating two indices and summing over all values of the repeated indices. Contraction reduces the tensor order by 2. When the contraction is conducted on all indices except the ith index on the tensor product of \mathbf{X} and \mathbf{Y} in $\mathbb{R}^{N_1 \times N_2 \times \cdots \times N_M}$, the contraction result can be denoted as

$$[\mathbf{X} \otimes \mathbf{Y}; (\bar{i}) (\bar{i})]$$

$$= [\mathbf{X} \otimes \mathbf{Y}; (1:i-1,i+1:M) (1:i-1,i+1:M)]$$

$$= \sum_{n_1=1}^{N_1} \cdots \sum_{n_{i-1}=1}^{N_{i-1}} \sum_{n_{i+1}=1}^{N_{i+1}} \cdots \sum_{n_M=1}^{N_M} \mathbf{X}_{n_1 \times \cdots \times n_{i-1} \times n_{i+1} \times \cdots \times n_M}$$

$$\times \mathbf{Y}_{n_1 \times \cdots \times n_{i-1} \times n_{i+1} \times \cdots \times n_M}$$

$$= \operatorname{mat}_i(\mathbf{X}) \operatorname{mat}_i^T(\mathbf{Y})$$

$$= X_i Y_i^T,$$
(2)

and $[\mathbf{X} \otimes \mathbf{Y}; (\bar{i})(\bar{i})] \in \mathbb{R}^{N_i \times N_i}$.

Definition 3 (mode-d matrix product). The mode-d matrix product defines multiplication of a tensor with a matrix in mode d. Let $\mathbf{X} \in \mathbb{R}^{N_1 \times \cdots \times N_M}$ and $A \in \mathbb{R}^{J \times N_d}$. Then, the $N_1 \times \cdots \times N_{d-1} \times J \times N_{d+1} \times \cdots \times N_M$ tensor is defined by

$$(\mathbf{X} \times_{d} A)_{N_{1} \times \dots \times N_{d-1} \times J \times N_{d+1} \dots \times N_{M}}$$

$$= \sum_{N_{d}} (\mathbf{X}_{N_{1} \times \dots \times N_{d} \dots \times N_{M}} A_{J \times N_{d}})$$

$$= [\mathbf{X} \otimes A; (d)(2)].$$
(3)

In this paper, we simplify the notation as

$$\mathbf{X} \times_1 A_1 \times_2 A_2 \times \dots \times A_M = \mathbf{X} \prod_{i=1}^M \times_i A_i, \tag{4}$$

$$\mathbf{X} \times_{1} A_{1} \times \cdots \times_{i-1} A_{i-1} \times_{i+1} A_{i+1} \times \cdots \times A_{M}$$

$$= \mathbf{X} \prod_{k=1, k \neq i}^{M} \times_{k} A_{k} = \mathbf{X} \overline{\times}_{i} A_{i}.$$
(5)

2.2. Principal component analysis with nonnegative and sparse constraint

The basic idea of PCA is to project the data along the directions of maximal variances so that the reconstruction error can be minimized. Let $x_1, \ldots, x_n \in \mathbb{R}^d$ form a zero mean collection of data points, arranged as the columns of the matrix $X \in \mathbb{R}^{d \times n}$, and let $u_1, \ldots, u_k \in \mathbb{R}^d$ be the principal vectors, arranged as the columns of the matrix $U \in \mathbb{R}^{d \times k}$. In [23], a new principal component analysis method

with nonnegative and sparse constraint is proposed, which is called NSPCA:

$$\max_{U} \frac{1}{2} ||U^{T}X||_{F}^{2} - \frac{\alpha}{4} ||I - U^{T}U||_{F}^{2} - \beta \mathbf{1}^{T}U\mathbf{1} \quad \text{s.t. } U \ge 0,$$
(6)

where $\|A\|_F^2$ is the square Frobenius norm, the second term relaxes the orthogonal constraint of traditional PCA, the third term is the sparse constraint, $\alpha > 0$ is a balancing parameter between reconstruction and orthogonality, $\beta \geq 0$ controls the amount of additional sparseness required.

2.3. Nonnegative tensor principal component analysis

In order to extend NSPCA in the tensor structure, we change the form of (6) since $||A||_F^2 = \text{tr}(AA^T)$ and Definition 3 and obtain following equation:

$$\max_{U \ge 0} \frac{1}{2} \operatorname{tr}(U^{T} X (U^{T} X)^{T}) - \frac{\alpha}{4} ||I - U^{T} U||_{F}^{2} - \beta \mathbf{1}^{T} U \mathbf{1}$$

$$= \max_{U \ge 0} \frac{1}{2} \operatorname{tr}\left(U^{T} \left(\sum_{i=1}^{n} X_{i} X_{i}^{T}\right) U\right)$$

$$- \frac{\alpha}{4} ||I - U^{T} U||_{F}^{2} - \beta \mathbf{1}^{T} U \mathbf{1}$$

$$= \max_{U \ge 0} \frac{1}{2} \sum_{i=1}^{n} \left[(X_{i} \times_{1} U^{T}) \otimes (X_{i} \times_{1} U^{T}); (1)(1) \right]$$

$$- \frac{\alpha}{4} ||I - U^{T} U||_{F}^{2} - \beta \mathbf{1}^{T} U \mathbf{1}.$$
(7)

Let \mathbf{X}_i denote the ith training sample with zero mean which is a tensor, and U_k is the kth projection matrix calculated by the alternating projection procedure. Here, \mathbf{X}_i ($0 \le i \le n$) are r-order tensors that lie in $\mathbb{R}^{N_1 \times N_2 \times \cdots N_r}$ and $U_k \in \mathbb{R}^{N_k^* \times N_k}$ ($k = 1, 2, \ldots, r$). Based on an analogy with (7), we define nonnegative tensor principal component analysis by replacing X_i with \mathbf{X}_i . So we can obtain the optimization problem as follows:

$$\max_{U_{1},\dots,U_{r}\geq 0} \frac{1}{2} \sum_{i=1}^{n} \left[\left(\mathbf{X}_{i} \prod_{k=1}^{r} \times_{k} U_{k}^{T} \right) \right.$$

$$\otimes \left(\mathbf{X}_{i} \prod_{k=1}^{r} \times_{k} U_{k}^{T} \right); (1:r)(1:r) \right] \qquad (8)$$

$$\left. - \frac{\alpha}{4} \sum_{k=1}^{r} \left| \left| I - U_{k}^{T} U_{k} \right| \right|_{F}^{2} - \beta \sum_{k=1}^{r} \mathbf{1}^{T} U_{k} \mathbf{1}.$$

In order to obtain the numerical solution of the problem defined in (8), we use the alternating projection method, which is an iterative procedure. Therefore, (8) is decomposed

into *r* different optimization subproblems as follows:

$$\max_{U_{l} \geq 0} \frac{1}{(l=1,...,r)} \frac{1}{2} \sum_{i=1}^{r} \left[\left(\mathbf{X}_{i} \prod_{k=1}^{r} \times_{k} U_{k}^{T} \right); \\
\otimes \left(\mathbf{X}_{i} \prod_{k=1}^{r} \times_{k} U_{k}^{T} \right) (1:r) (1:r) \right] \\
- \frac{\alpha}{4} \sum_{k=1}^{r} ||I - U_{k}^{T} U_{k}||_{F}^{2} - \beta \sum_{k=1}^{r} \mathbf{1}^{T} U_{k} \mathbf{1} \\
= \max_{U_{l} \geq 0} \frac{1}{(l=1,...,r)} \frac{1}{2} \sum_{i=1}^{n} \left[\left(\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T} \times_{l} U_{l}^{T} \right) \\
\otimes \left(\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T} \times_{l} U_{l}^{T} \right); (1:r) (1:r) \right] \\
- \frac{\alpha}{4} ||I - U_{l}^{T} U_{l}||_{F}^{2} - \beta \mathbf{1}^{T} U_{l} \mathbf{1} \\
= \max_{U_{l} \geq 0} \frac{1}{(l=1,...,r)} \frac{1}{2} \operatorname{tr} \left(U_{l}^{T} \left(\sum_{i=1}^{n} \left[\operatorname{mat}_{l} \left(\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T} \right) \right] \right) U_{l} \right) \\
\times \operatorname{mat}_{l}^{T} \left(\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T} \right) \right] \right) U_{l} \right) \\
- \frac{\alpha}{4} ||I - U_{l}^{T} U_{l}||_{F}^{2} - \beta \mathbf{1}^{T} U_{l} \mathbf{1} \\
- \frac{\alpha}{4} \sum_{k=1, k \neq l}^{r} ||I - U_{k}^{T} U_{k}||_{F}^{2} - \beta \sum_{k=1, k \neq l}^{r} \mathbf{1}^{T} U_{k} \mathbf{1}.$$
(9)

In order to simplify (9) we define

$$A_{l} = \sum_{i=1}^{n} \left[\operatorname{mat}_{l}(\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T}) \operatorname{mat}_{l}^{T} (\mathbf{X}_{i} \overline{\times}_{l} U_{l}^{T}) \right],$$

$$C_{l} = -\frac{\alpha}{4} \sum_{k=1, k \neq l}^{r} \left| \left| I - U_{k}^{T} U_{k} \right| \right|_{F}^{2} - \beta \sum_{k=1, k \neq l}^{r} \mathbf{1}^{T} U_{k} \mathbf{1}.$$

$$(10)$$

Therefore, (9) becomes

$$\max_{U_{l} \ge 0} \frac{1}{(l=1,\dots,r)} \frac{1}{2} ||U_{l}^{T} B_{l}||_{F}^{2} - \frac{\alpha}{4} ||I - U_{l}^{T} U_{l}||_{F}^{2} - \beta \mathbf{1}^{T} U_{l} \mathbf{1} + C_{l},$$
(11)

where $A_l = B_l B_l^T$. But as described in [23], the above optimization problem is a concave quadratic programming, which is an NP-hard problem. Therefore, it is unrealistic to find the global solution of (11), and we have to settle with a local maximum. Here we give a function of u_{lpq} as the optimization objective

$$f(u_{lpq}) = -\frac{\alpha}{4}u_{lpq}^4 + c_2u_{lpq}^2 + c_1u_{lpq} + \text{const},$$
 (12)

```
Input: Training tensor \mathbf{X}_j \in \mathbb{R}^{N_1 \times N_2 \times \cdots N_r}, (1 \le j \le n), the dimensionality of the output tensors
\mathbf{Y}_i \in \mathbb{R}^{N_1^* \times N_2^* \times \cdots N_r^*}, \alpha, \beta, maximum number of training iterations T, error threshold \varepsilon.
Output: The projection matrix U_l \ge 0 (l = 1, ..., r), the output tensors Y_i.
Initialization: Set U_l^{(0)} \ge 0 (l = 1, ..., r) randomly, iteration index t = 1.
            Repeat until convergence {
                For l = 1 to r {
Step 2.
                   Calculate \mathbf{A}_{l}^{(t-1)};
Step 3.
                   Iterate over every entries of U_l^{(t)} until convergence
Step 4.
                      – Set the value of u_{lpq} to the global nonnegative maximizer of
                      (12) by evaluating it over all nonnegative roots of
                      (14) and zero;
Step 5.
                   Check convergence: the training stage of NTPCA convergence
                         if t > T or update error e < \varepsilon
           \mathbf{Y}_{i} = \mathbf{X}_{i} \prod_{l=1}^{r} \times_{l} U_{l}
```

ALGORITHM 1: Alternating projection optimization procedure for NTPCA.

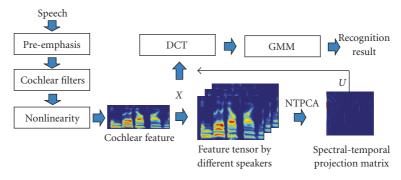


FIGURE 1: Feature extraction and recognition framework.

where const is the independent term of u_{lpq} and

$$c_{1} = \sum_{i=1, i \neq q}^{d} a_{lsi} u_{lpi} - \alpha \cdot \sum_{i=1, i \neq p}^{k} \sum_{j=1, j \neq q}^{d} u_{lpj} u_{lij} u_{liq} - \beta,$$

$$c_{2} = a_{lqq} + \alpha - \alpha \cdot \sum_{i=1, i \neq q}^{d} u_{lpi}^{2} - \alpha \cdot \sum_{i=1, i \neq p}^{k} u_{liq}^{2},$$
(13)

where a_{lij} is the element of A_l . Setting the derivative with respect to u_{lpq} to zero, we obtain a cubic equation

$$\frac{\partial f}{\partial u_{lpq}} = -\alpha u_{lpq}^3 + c_2 u_{lpq} + c_1 = 0. \tag{14}$$

We calculate the nonnegative roots of (14) and zero as the nonnegative global maximum of $f(u_{lpq})$. Algorithm 1 lists the alternating projection optimization procedure for Nonnegative Tensor PCA.

3. AUDITORY FEATURE EXTRACTION BASED ON TENSOR STRUCTURE

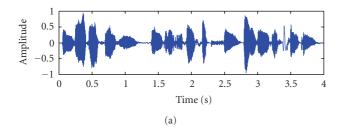
The human auditory system can accomplish the speaker recognition easily and be insensitive to the background noise.

In our feature extraction framework, the first step is to obtain the frequency selectivity information by imitating the process performed in the auditory periphery and pathway. And then we represent the robust speech feature as the extracted auditory information mapped into multiple interrelated feature subspace via NTPCA. A diagram of feature extraction and speaker recognition framework is shown in Figure 1.

3.1. Feature extraction based on auditory model

We extract the features by imitating the process occurred in the auditory periphery and pathway, such as outer ear, middle ear, basilar membrane, inner hair cell, auditory nerves, and cochlear nucleus.

Because the outer ear and the middle ear together generate a bandpass function, we implement traditional preemphasis to model the combined outer and middle ear functions $x_{\rm pre}(t) = x(t) - 0.97x(t-1)$, where x(t) is the discrete-time speech signal, $t = 1, 2, \ldots$, and $x_{\rm pre}(t)$ is the filtered output signal. Its purpose is to raise the energy for those frequency components located in the high-frequency domain in order that those formants can be extracted in the high-frequency domain.



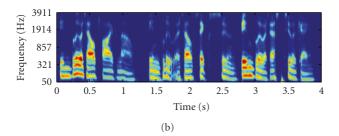


FIGURE 2: Clean speech sentence and illustrations of cochlear power feature. Note the asymmetric frequency resolution at low and high frequencies in the cochlear.

The frequency selectivity of peripheral auditory system such as basilar membrane is simulated by a bank of cochlear filters. The cochlear filterbank represents frequency selectivity at various locations along the basilar membrane in a cochlea. The "gammatone" filterbanks implemented by Slaney [24] are used in this paper, which have an impulse response in the following form:

$$g_i(t) = a_i t^{n-1} e^{2\pi b_i \text{ERB}(f_i)t} \cos(2\pi f_i t + \phi_i) \quad (1 \le i \le N),$$
(15)

where n is the order of the filter, N is the number of filterbanks. For the ith filter bank, f_i is the center frequency, ERB(f_i) = 24.7(4.37 f_i /1000 + 1) is the equivalent rectangular bandwidth (ERB) of the auditory filter, ϕ_i is the phase, $a_i, b_i \in \mathbb{R}$ are constants, where b_i determines the rate of decay of the impulse response, which is related to bandwidth. The outputs of each gammatone filterbank is $x_g^i(t) = \sum_{\tau} x_{\text{pre}}(\tau) g_i(t-\tau)$.

In order to model nonlinearity of the inner hair cells, we compute the power of each band in every frame k with a logarithmic nonlinearity

$$P(i,k) = \log\left(1 + \gamma \sum_{t \in \text{frame } k} \left\{x_g^i(t)\right\}^2\right),\tag{16}$$

where P(i,k) is the output power, γ is a scaling constant. This model can be considered as average firing rates in the inner hair cells, which simulate the higher auditory pathway. The resulting power feature vector P(i,k) at frame k with component index of frequency f_i comprises the spectrotemporal power representation of the auditory response. Figure 2 presents an example of clean speech utterance (sampling rate 8 kHz) and corresponding illustrations of the cochlear power feature in the spectrotemporal domain. Similar to mel-scale

processing in MFCC extraction, this power spectrum provides a much higher frequency resolution at low frequencies than at high frequencies.

3.2. Sparse representation based on tensor structure

In order to extract robust feature based on tensor structure, we model the cochlear power feature of different speakers as 3-order tensor $\mathbf{X} \in \mathbb{R}^{N_f \times N_t \times N_s}$. Each feature tensor is an array with three models $frequency \times time \times speaker identity$ which comprises the cochlear power feature matrix $X \in \mathbb{R}^{N_f \times N_t}$ of different speakers. Then we transform the auditory feature tensor into multiple interrelated subspaces by NTPCA to learn the projection matrices U_l (l=1,2,3). Figure 3 shows the tensor model for projection matrices calculation. Compared with traditional subspace learning methods, the extracted tensor features may characterize the differences of speakers and preserve the discriminative information for classification.

As described in Section 3.1, the cochlear power feature can be considered as neuron response in the inner hair cells, and hair cells have receptive fields which refer to a coding of sound frequency. Recently, a sparse coding for sound based on skewness maximization [15] was successfully applied to explain the characteristics of sparse auditory receptive fields. And here we employ the sparse localized projection matrix $U \in \mathbb{R}^{d \times N_f}$ in time-frequency subspace to transform the auditory feature into the sparse feature subspace, where d is the dimension of sparse feature subspace. The auditory sparse feature representation X_s is obtained via the following transformation:

$$X_{\rm s} = UX. \tag{17}$$

Figure 4(a) shows an example of projection matrix in spectrotemporal domain. From this result we can see that most elements of this project matrix are near to zero, which accords with the sparse constraint of NTPCA. Figure 4(b) gives several samples for coefficients of feature vector after projection, which also prove the sparse characteristic of feature.

For the final feature set, we apply discrete cosine transform (DCT) on the feature vector to reduce the dimensionality and decorrelate feature components. A vector of cepstral coefficients $X_{\text{ceps}} = CX_s$ is obtained from sparse feature representation X_s , where $C \in \mathbb{R}^{Q \times d}$ is discrete cosine transform matrix.

4. EXPERIMENTS AND DISCUSSION

In this section, we describe the evaluation results of a close-set speaker identification system using ANTCC feature. Comparisons with MFCC, LPCC, and RASTA-PLP features are also provided.

4.1. Clean data evaluation

The first stage is to evaluate the performance of different speaker identification methods in the two clean speech datasets: Grid and TIMIT.

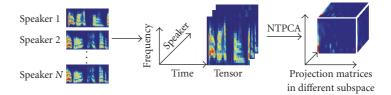


FIGURE 3: Tensor model for calculation of projection matrices via NTPCA.

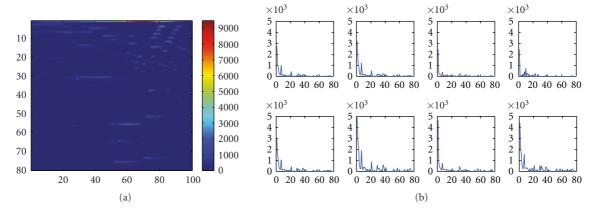


FIGURE 4: (a) Projection matrix (80 × 100) in spectrotemporal domain. (b) Samples for sparse coefficients (encoding) of feature vector.

For Grid dataset, there are 17 000 sentences spoken by 34 speakers (18 males and 16 females). In our experiment, the sampling rate of speech signals was 8 kHz. For the given speech signals, we employed every window of length 8000 samples (1 second) and time duration 20 samples (2.5 milliseconds) and 36 gammatone filters were selected. We calculated the projection matrix in spectrotemporal domain using NTPCA after the calculation of the average firing rates in the inner hair cells. 170 sentences (5 sentences each person) were selected randomly as the training data for learning projection matrices in different subspaces. 1700 sentences (50 sentences each person) were used as training data and 2040 sentences (60 sentences each person) were used as testing data.

TIMIT is a noise-free speech database recorded with a high-quality microphone sampled at 16 kHz. In this paper, randomly selected 70 speakers in the train folder of TIMIT were used in the experiment. In TIMIT, each speaker produces 10 sentences, the first 7 sentences were used for training, and the last 3 sentences were used for testing, which were about 24 s of speech for training and 6 s for testing. For the projection matrix learning, we select 350 sentences (5 sentences each person) as training data and the dimension of sparse tensor representation is 32.

We use 20 coefficient feature vectors in all our experiments to keep a fair comparison. The classification engine used in this experiment was based on a 16, 32, 64, and 128 mixtures GMM classifier. Table 1 presents the identification accuracy obtained by the various features in clean condition.

From the simulation results, we can see that all the methods can give a good performance for the Grid dataset with different Gaussian mixture numbers. For the TIMIT

Table 1: Identification accuracy with different mixture numbers for clean data of Grid and TIMIT datasets.

Features	Grid(%)				TIMIT(%)			
reatures	16	32	64	128	16	32	64	128
ANTCC	99.9	100	100	100	96.5	97.62	98.57	98.7
LPCC	100	100	100	100	97.6	98.1	98.1	98.1
MFCC	100	100	100	100	98.1	98.1	98.57	99
PLP	100	100	100	100	89.1	92.38	90	93.1

dataset, MFCC also represents a good performance on the testing conditions. And ANTCC feature provides the same performance as MFCC when the Gaussian mixture number increases. This may indicate that the distribution of ANTCC feature is sparse and not smooth, which causes the performance to degrade when the Gaussian mixture number is too small. So we have to increase Gaussian mixture number to fit its actual distribution.

4.2. Performance evaluation under different noisy environments

In consideration of practical applications of robust speaker identification, different noise classes were considered to evaluate the performance of ANTCC against the other commonly used features and identification accuracy was assessed again. Noise samples for the experiments were obtained from Noisex-92 database. The noise clippings were added to clean speech obtained from Grid and TIMIT datasets to generate testing data.

Table 2: Identification accuracy	in four noisy conditions (white,
pink, factory, and f16) for Grid da	ataset.

(%)	SNR	ANTCC	GMM-UBM	MFCC	LPCC	RASTA-PLP
	0 dB	10.29	3.54	2.94	2.45	9.8
	5 dB	38.24	13.08	9.8	3.43	12.25
	$10\mathrm{dB}$	69.61	26.5	24.02	8.82	24.51
	15 dB	95.59	55.29	42.65	25	56.37
	0 dB	9.31	10.67	16.67	7.35	10.29
Pink	5 dB	45.1	21.92	28.92	15.69	24.51
	10 d	87.75	54.51	49.51	37.25	49.02
	15 d	95.59	88.09	86.27	72.55	91.18
Factory	0 dB	8.82	11.58	14.71	9.31	11.27
	5 dB	44.61	41.92	35.29	25	29.9
	10 d	87.75	60.04	66.18	52.94	63.24
	15 d	97.55	88.2	92.65	87.75	96.57
F16	0 dB	9.8	8.89	7.35	7.84	12.25
	5 dB	27.49	15.6	12.75	15.2	26.47
	10 d	69.12	45.63	52.94	36.76	50
	15 d	95.1	82.4	76.47	63.73	83.33

4.2.1. Grid dataset in noisy environments

Table 2 shows the identification accuracy of ANTCC at various SNRs (0 dB, 5 dB, 10 dB, and 15 dB) with white, pink, factory, and f16 noises. For the projection matrix and GMM speaker model training, we use the similar setting as clean data evaluation for Grid dataset. For comparison, we implement an GMM-UBM system using MFCC feature. 256-mixture UBM is created for TIMIT dataset and Grid dataset is used for GMM training and testing.

From the identification comparison, the performance under Gaussian white additive noise indicates that ANTCC is the predominant feature and topping to 95.59% under SNR of 15 dB. However, it is not recommended for noise level less than 5 dB SNR where the identification rate becomes less than 40%. RASTA-PLP is the second-best feature, yet it yields 56.37% less than ANTCC under 15 dB SNR.

Figure 5 describes the identification rate in four noisy conditions averaged over SNRs between 0 and 15 dB, and the overall average accuracy across all the conditions. ANTCC under different noise conditions, respectively, showed better average performance than the other features, indicating the potential of the new feature for dealing with a wider variety of noisy conditions.

4.2.2. TIMIT dataset in noisy environments

For speaker identification experiments that were conducted using TIMIT dataset with different additive noise, the general setting was almost the same as that used with clean TIMIT dataset.

Table 3 shows the identification accuracy comparison using four features with GMM classifiers. The results show that ANTCC feature demonstrates good performance in the presence of four noises. Especially for the white and

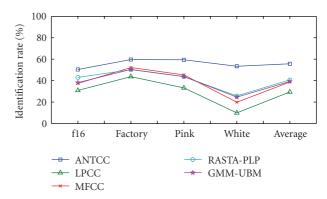


FIGURE 5: Identification accuracy in four noisy conditions averaged over SNRs between 0 and 15 dB, and the overall average accuracy across all the conditions, for ANTCC and other features using Grid dataset mixed with additive noises.

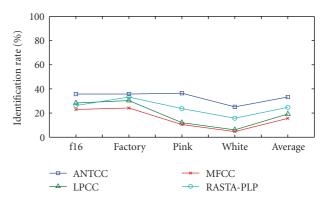


FIGURE 6: Identification accuracy in four noisy conditions averaged over SNRs between 0 and 15 dB, and the overall average accuracy across all the conditions, for ANTCC and other three features using TIMIT dataset mixed with additive noises.

pink noise, ANTCC improves average accuracy by 21% and 16% compared with other three features, which indicate the stationary noise components are suppressed after the multiple interrelated subspace projection. From Figure 6, we can see that the average identification rate confirm again that ANTCC feature is better than all other features.

4.2.3. Aurora2 dataset evaluation result

Aurora2 dataset is designed to evaluate the performance of speech recognition algorithms in noisy conditions. In the training set, there are 110 speakers (55 males and 55 females) with clean and noisy speech data. In our experiments, the sampling rate of speech signals was 8 kHz. For the given speech signals, we employed time window of length 8000 samples (1 second) and time duration 20 samples (2.5 millisecond) and 36 cochlear filterbanks. As described above, we calculated the projection matrix using NTPCA after the calculation of cochlear power feature. 550 sentences (5 sentences each person) were selected randomly as the training data for learning projection matrix in different subspaces and 32 dimension sparse tensor representation are extracted.

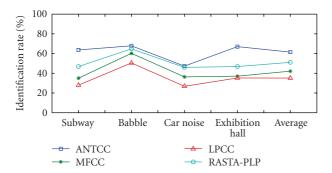


FIGURE 7: Identification accuracy in four noisy conditions averaged over SNRs between 5 and 20 dB, and the overall average accuracy across all the conditions, for ANTCC and other three features using Aurora2 noise testing dataset.

In order to estimate the speaker model and test the efficiency of our method, we used 5500 sentences (50 sentences each person) as training data and 1320 sentences (12 sentences each person) mixed with different kinds of noise were used as testing data. The testing data was mixed with subway, babble, car noise, and exhibition hall in SNR intensities of 20 dB, 15 dB, 10 dB, and 5 dB. For the final feature set, 16 cepstral coefficients were extracted and used for speaker modeling.

For comparison, the performance of MFCC, LPCC, and RASTA-PLP with 16-order cepstral coefficients was also tested. GMM was used to build the recognizer with 64 Gaussian mixtures. Table 4 presents the identification accuracy obtained by ANTCC and baseline system in all testing conditions. We can observe from Table 4 that the performance degradation of ANTCC is slower with noise intensity increase compared with other features. It performs better than other three features in the high-noise conditions such as 5 dB condition noise.

Figure 7 describes the average accuracy in all noisy conditions. The results suggest that this auditory-based tensor representation feature is robust against the additive noise and suitable to the real application such as handheld devices or Internet.

4.3. Discussion

In our feature extraction framework, the preprocessing method is motivated by the auditory perception mechanism of human being which simulates a cochlear-like peripheral auditory stage. The cochlear-like filtering uses the ERB, which compresses the information in high-frequency region. So such feature can provide a much higher frequency resolution at low frequencies as shown in Figure 1(b).

NTPCA is applied to extract the robust feature by calculating projection matrices in multirelated feature subspace. This method is a supervised learning procedure which preserves the individual, spectrotemporal information in the tensor structure.

Our feature extraction model is a noiseless model, and here we add sparse constraints to NTPCA. It is based on the fact that in sparse coding the energy of the signal is

Table 3: Identification accuracy in four noisy conditions (white, pink, factory, and f16) for TIMIT dataset.

(%)	SNR	ANTCC	MFCC	LPCC	RASTA-PLP
White	0 dB	2.9	1.43	2.38	2.38
	5 dB	3.81	2.38	2.86	5.24
	10 dB	29.52	3.33	6.19	15.71
	15d B	64.29	11.43	12.86	39.52
	0 dB	2.43	1.43	3.33	1.43
Pink	5 dB	13.81	1.9	3.81	5.24
FIIIK	10 d	50.95	8.57	8.1	27.14
	15 d	78.57	30	32.86	60.95
	0 dB	2.43	1.43	2.76	1.43
Eactory	5 dB	12.86	3.33	10.48	10
Factory	10 d	49.52	21.9	34.29	46.67
	15 d	78.1	70	73.81	74.76
F16	0 dB	2.9	2.86	2.33	1.43
	5 dB	15.24	7.14	14.76	8.1
	10 d	47.14	24.76	28.57	34.76
	15 d	77.62	57.14	67.62	60.48

Table 4: Identification accuracy in four noisy conditions (subway, car noise, babble, and exhibition hall) for Aurora2 noise testing dataset.

(%)	SNR	ANTCC	MFCC	LPCC	RASTA-PLP
	5 dB	26.36	2.73	5.45	14.55
Subway	10 dB	63.64	16.36	11.82	39.09
Subway	15 dB	75.45	44.55	34.55	57.27
	20 dB	89.09	76.36	60.0	76.36
	5 dB	43.27	16.36	15.45	22.73
Babble	10 dB	62.73	51.82	33.64	57.27
Daobic	15 dB	78.18	79.09	66.36	86.36
	20 dB	87.27	93.64	86.36	92.73
	5 dB	19.09	5.45	3.64	8.18
Car noise	10 dB	30.91	17.27	10.91	35.45
Cai noise	15 dB	60.91	44.55	33.64	60.91
	20 dB	78.18	78.18	59.09	79.45
	5 dB	24.55	1.82	2.73	13.64
Exhibition hall	10 dB	62.73	20.0	19.09	31.82
Lamordon Hall	15 dB	85.45	50.0	44.55	59.09
	20 dB	95.45	76.36	74.55	82.73

concentrated on a few components only, while the energy of additive noise remains uniformly spread on all the components. As a soft-threshold operation, the absolute values of pattern from the sparse coding components are compressed towards to zero. The noise is reduced while the signal is not strongly affected. We also employ the variance maximum criteria to extract the helpful feature in principal component subspace for identification. The noise component will be removed as the useless information in minor components subspace.

From Section 4.1, we know the performance of ANTCC in clean speech is not better than conventional feature MFCC

and LPCC when the speaker model estimation with few Gaussian mixtures. The main reason is that the sparse feature does not have the smoothness property as MFCC and LPCC. We have to increase the Gaussian mixture number to fit its actual distribution.

5. CONCLUSIONS

In this paper, we presented a novel speech feature extraction framework which is robust to noise with different SNR intensities. This approach is primarily data driven and is able to extract robust speech feature called ANTCC, which is invariant to noise types and interference with different intensities. We derived new feature extraction methods called NTPCA for robust speaker identification. The study is mainly focused on the encoding of speech based on general higher-order tensor structure to extract the robust auditory-based feature from interrelated feature subspace. The frequency selectivity features at basilar membrane and inner hair cells were used to represent the speech signals in the spectrotemporal domain, and then NTPCA algorithm was employed to extract the sparse tensor representation for robust speaker modeling. The discriminative and robust information of different speakers may be preserved after the multirelated subspace projection. Experimental results on three datasets showed that the new method improved the robustness of feature, in comparison to baseline systems trained on the same speech datasets.

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